

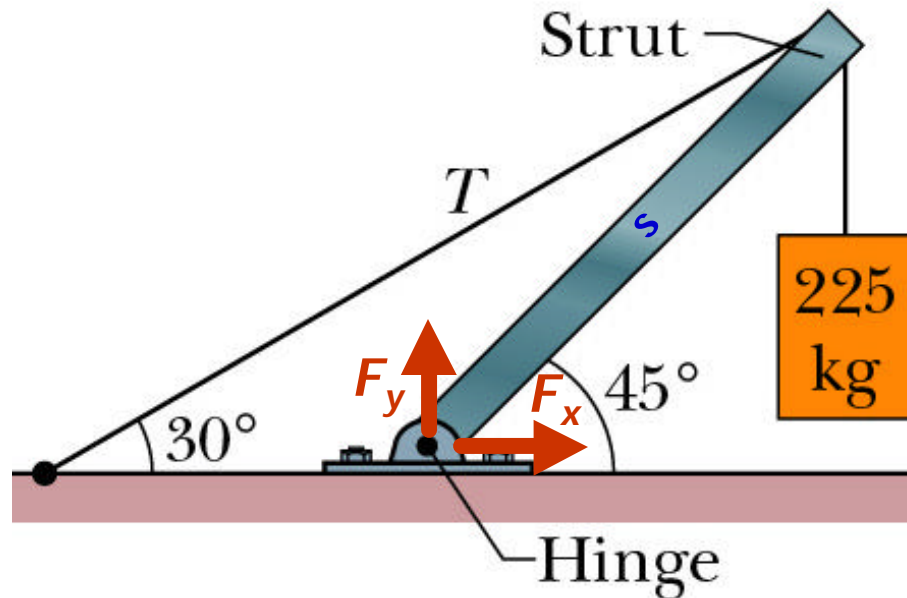
Remember

- Midterm 2 to be taken one week from today
- Will cover mainly chapter 7 - 13
 - ◆ But understanding previous chapters may be needed
- Check website at **Exam Specifics for midterm 2
 - ◆ Practice exam and solutions
 - ◆ Exam Guide
- Important issue is to be able to do problems

Today

- Hand in HW 7
- Finish chapter 13 ...
 - ◆ Ch 7 - 13 emphasized in midterm 2
- Go on to gravity

Problem 13-25 (not assigned)

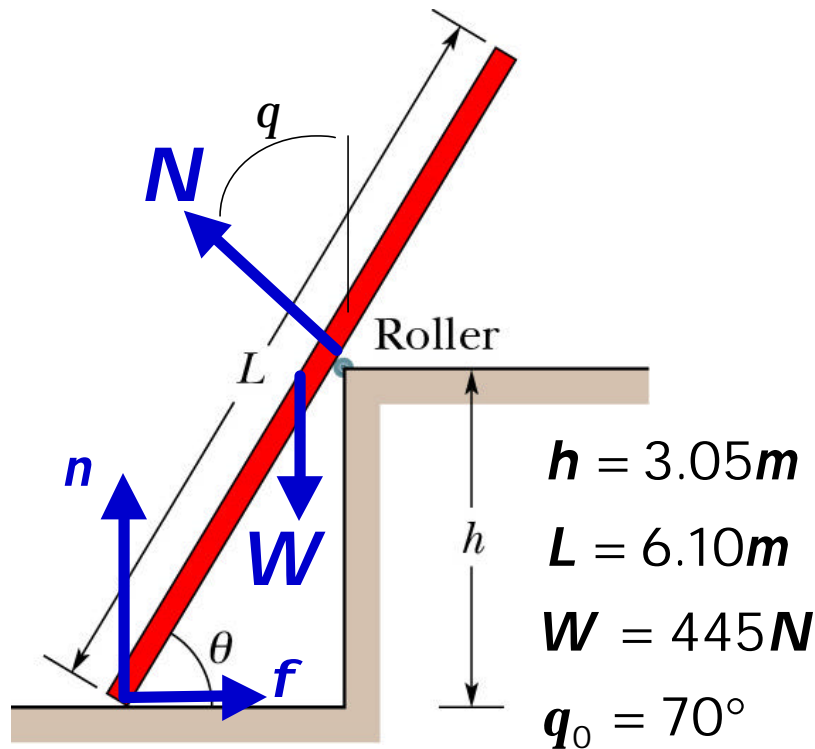


- **Strut $M_s = 45\text{kg}$**
 - ◆ **Take length s**
- **Find**
 - ◆ **tension, T**
 - ◆ **Force components at the hinge**

The system is in equilibrium. A concrete block of mass 225 kg hangs from the end of the uniform strut whose mass is 45.0 kg. Find

- the tension T in the cable and the
- horizontal and
- vertical force components on the strut from the hinge.

Problem 13-29 (not assigned)



A uniform plank, with a length L of 6.10 m and a weight of 445 N, rests on the ground and against a frictionless roller at the top of a wall of height $h = 3.05$ m. The plank remains in equilibrium for any value of $q > 70^\circ$ but slips if $q < 70^\circ$.

Find the coefficient of static friction between the plank and the ground.

- Frictionless at the roller
- Find that if $q < q_0$, the plank slips
- What is m_s for the plank contact with ground?

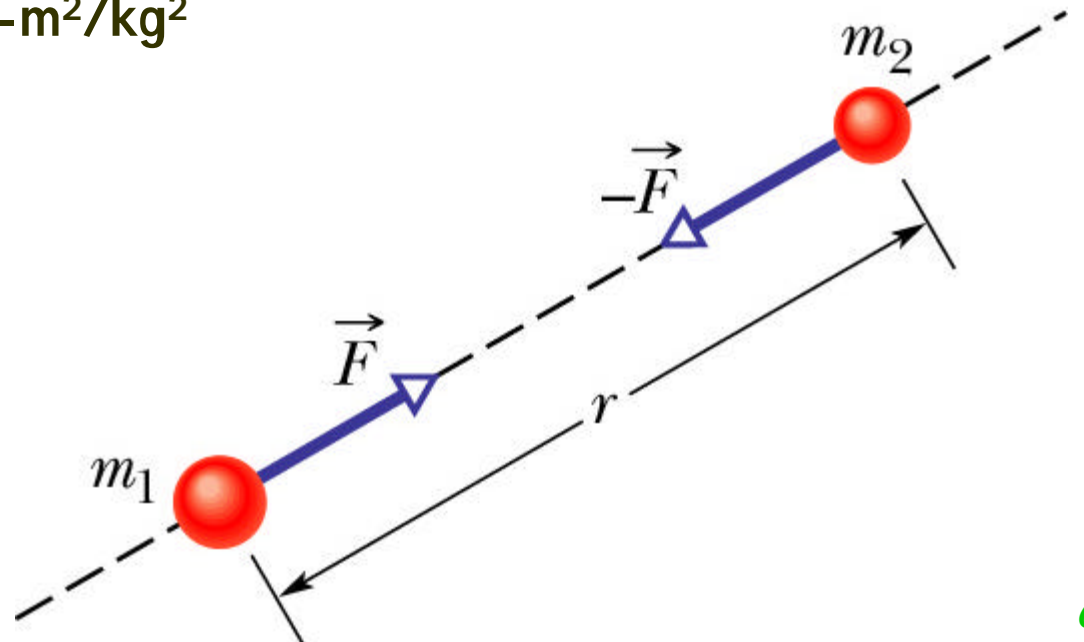
Ch 14 - Gravitation

- Newton's great achievements of late 17th century science
 - ◆ 3 laws of motion
 - To some extent, were re-statements by Galileo and others
 - ◆ law of universal gravitation
 - unique and important essential to complete the picture
- Thus far, we have only seen the utility of Newton's Laws in describing everyday laws (on Earth's surface)
 - ◆ investigated by many: Galileo, Toricelli, ...
- Truly earthshaking discovery was supplementing this with the Universal Law of Gravitation
 - ◆ lots of competition: Hooke, ...
 - ◆ explained astronomical descriptions of Solar system +

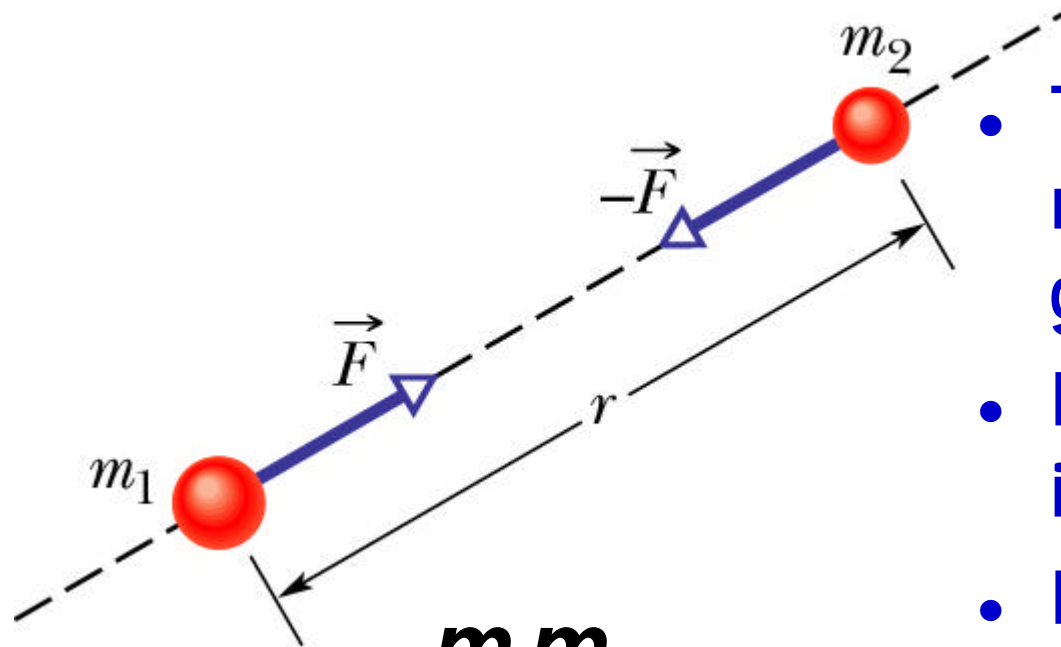
What is Gravity? (Newton)

- Attractive force between any two mass elements of the universe; force is:
 - ◆ always attractive
 - ◆ proportional to masses
 - ◆ inversely proportional to square of separation
 - ◆ dependent on a new universal constant, G
 - $G = 6.67 \cdot 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2$

$$F = G \frac{m_1 m_2}{r^2}$$



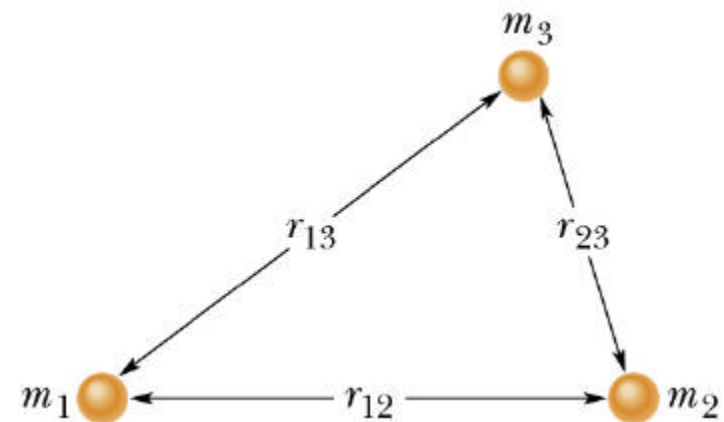
Gravity Potential Energy



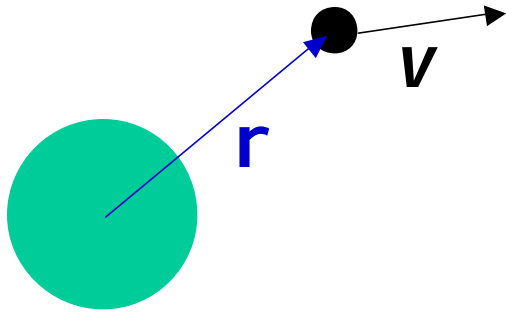
- This must be the right potential ... it gives the right force
- Note path independence ...
- Note text examples

$$U = -G \frac{m_1 m_2}{r}$$

$$F_r = - \frac{dU}{dr} = -G \frac{m_1 m_2}{r^2}$$



Energies of Any Body and Escape Velocity



- Note that $E < 0$ corresponds to bound body (planet, etc)
- $E > 0$ is unbound body
- Escape from surface of Earth requires $E > 0$

$$K = \frac{1}{2} mv^2$$

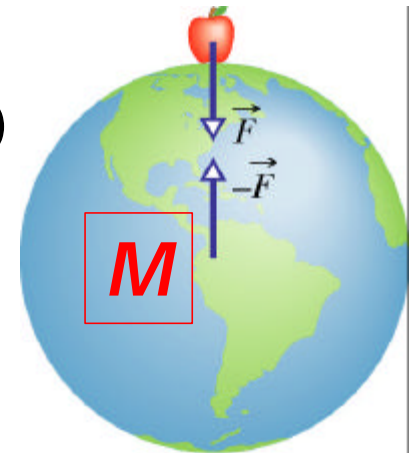
$$U = -G \frac{Mm}{r}$$

$$E = K + U = \text{const.}$$

$$E > 0$$

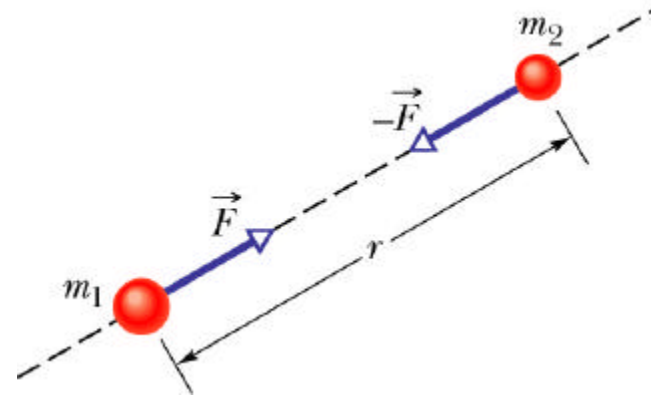
$$\frac{1}{2} mv_{\text{esc}}^2 - G \frac{Mm}{R} = 0$$

$$v_{\text{esc}} = \sqrt{\frac{2GM}{R}}$$



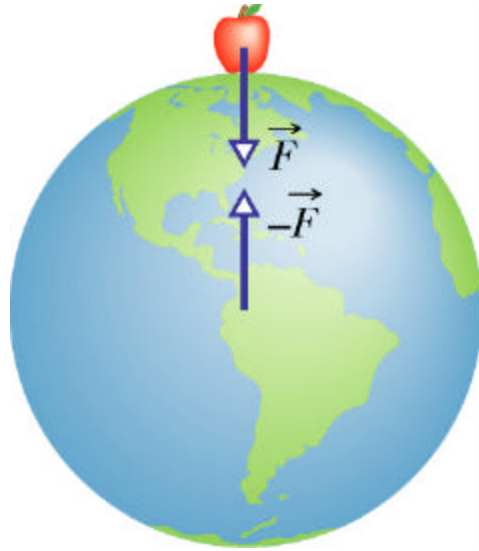
Applicability of Newton's Gravity

$$F = G \frac{m_1 m_2}{r^2}$$



- Still (with modifications from General Relativity) accepted as the basic force law
- Applies in all known circumstances
 - ◆ Earth's surface
 - ◆ Inside the Earth
 - ◆ Solar System
 - ◆ Grand Universe...
- Important general law of force
- Similar form for electricity, ...

Gravity at surface of the Earth



$$G \frac{Mm}{R^2} = mg$$

$$g = G \frac{M}{R^2}$$

$M = \text{Earth mass}$
 $R = \text{Earth radius}$
 $G = \text{universal gravitational constant}$

- Many subtleties

- ◆ Density vs r (look into here)
- ◆ Rotation of Earth (small)
- ◆ slightly nonspherical shape
- ◆ ...

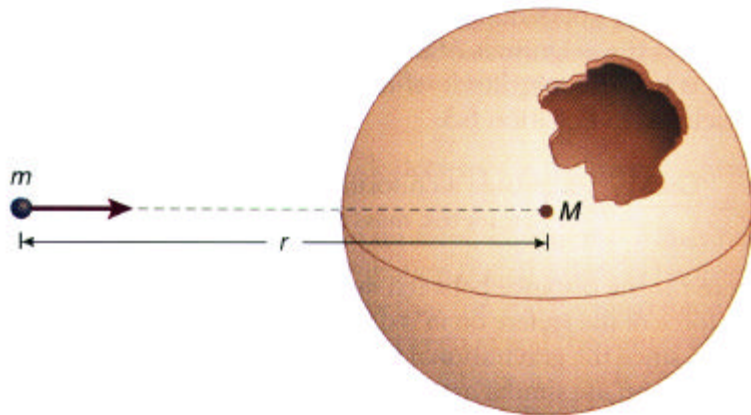
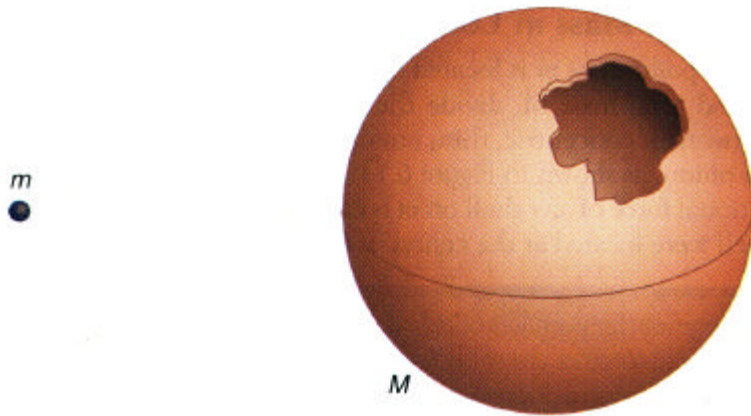
- ALL SMALL!!

- Assertion

- ⊖ All mass of Earth can be considered to be at the center when seen from outside
- ⊖ Can be proven!
- ⊖ Unexpected result for force on object inside Earth

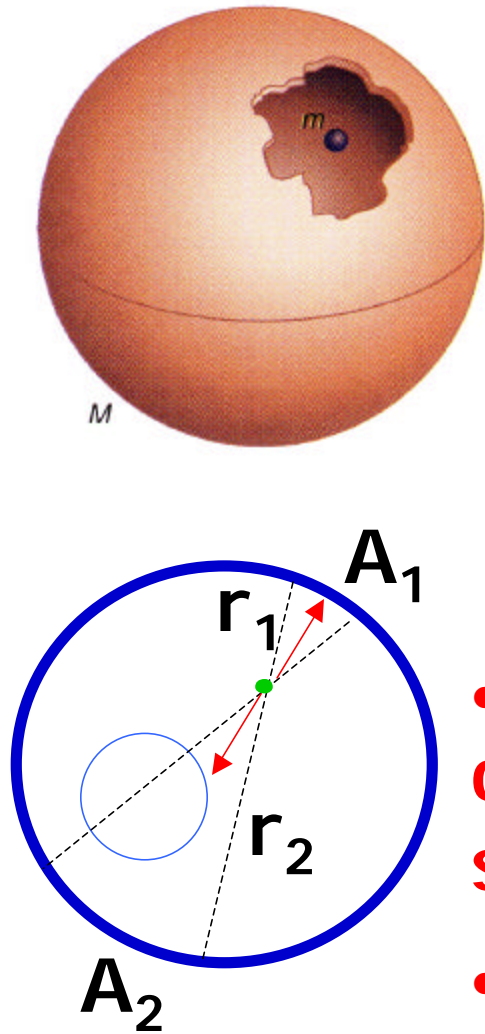
Shell of Mass from OUTSIDE

- Force on m is as if all the mass M were concentrated at the center of the sphere
♦ *ie*, at center of mass



$$F = G \frac{mM}{r^2}$$

Shell of Mass from INSIDE



$$\frac{A_2}{A_1} = \frac{r_2^2}{r_1^2}$$

$$\frac{F_2}{F_1} = \frac{\frac{A_2}{r_2^2}}{\frac{A_1}{r_1^2}} = \frac{A_2}{A_1} \frac{r_1^2}{r_2^2} = 1$$

• Forces on m from opposite pieces of surface cancel

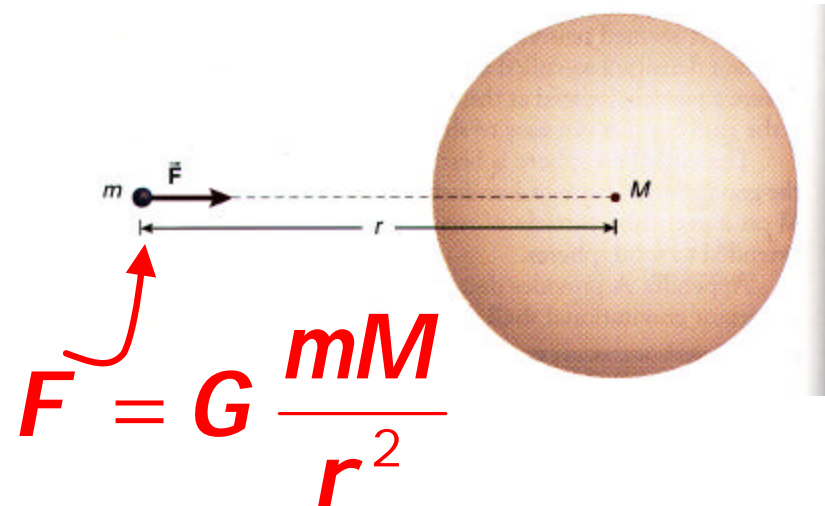
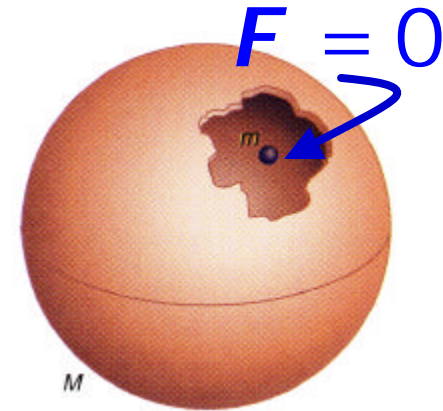
• No net force on m INSIDE shell!

- cone through m intercepts the sphere in two places
- Area on shell surface intercepted by cone $\sim r^2$
- Magnitudes of forces on m by pieces of surface 1, 2

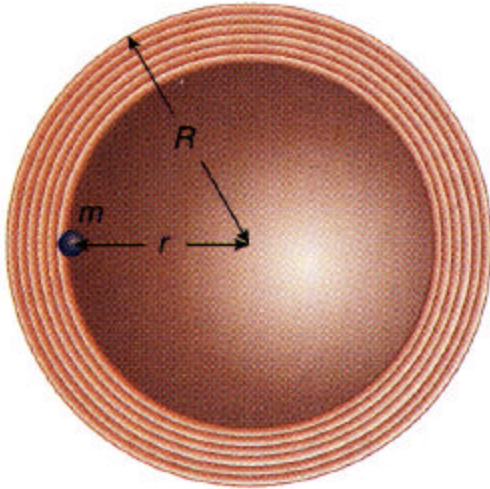
$$F_{1,2} = G \frac{mm_{1,2}}{r_{1,2}^2}$$

Shell of Mass from INSIDE and OUTSIDE

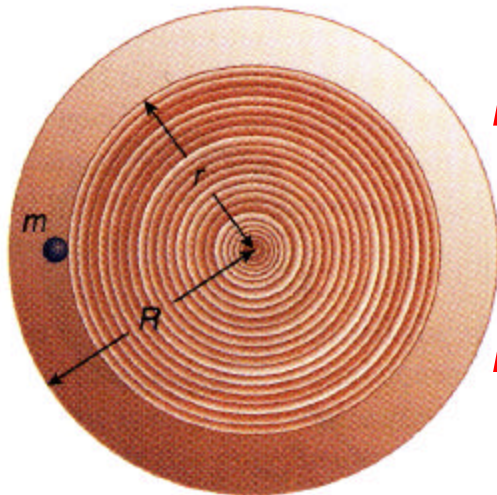
- Summarize: for a uniform shell of mass
 - ◆ Any mass inside feels no force
 - ◆ Any mass outside feels a force as if all of M were concentrated at center of the sphere (shell)
- Can be proven in each case mathematically by integrating over all the mass in the shell
 - ◆ Try if you like!



Consider Earth as continuous, uniform set of shells



- Shells outside ($r > R$) contribute NO net force on m
- Shells inside ($r < R$) act as if all their mass concentrated at the center
- Only that part of the Earth mass inside r is relevant to the force on m
- Check out problem 14-23



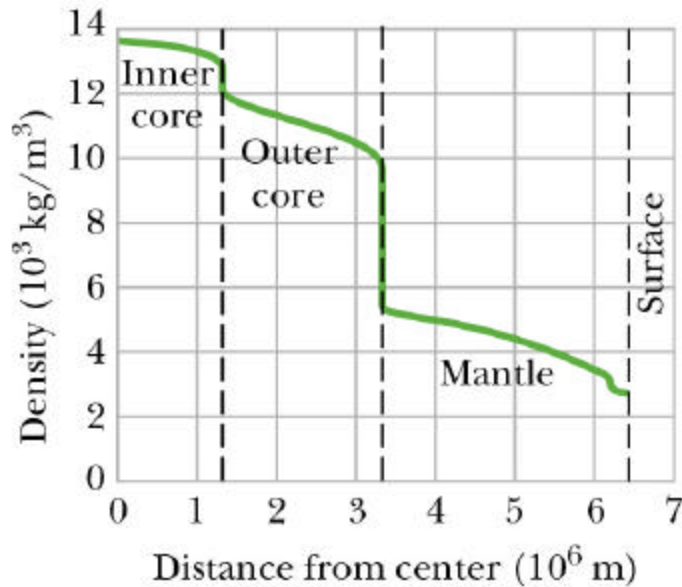
$$F = G \frac{mM_{\text{inside } m}}{r^2}$$

Actually Earth not uniform (next slide) but general point valid

$$F = G \frac{m}{r^2} M_{\text{tot}} \frac{\frac{4}{3}pr^3}{\frac{4}{3}pR^3} = \left[G \frac{mM_{\text{tot}}}{R^3} \right] r$$

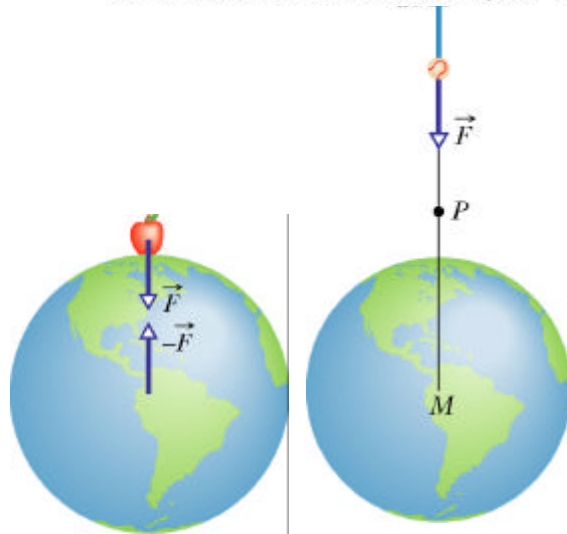
attractive to center ... like spring force

Earth Structure and Empirical "Gravity"



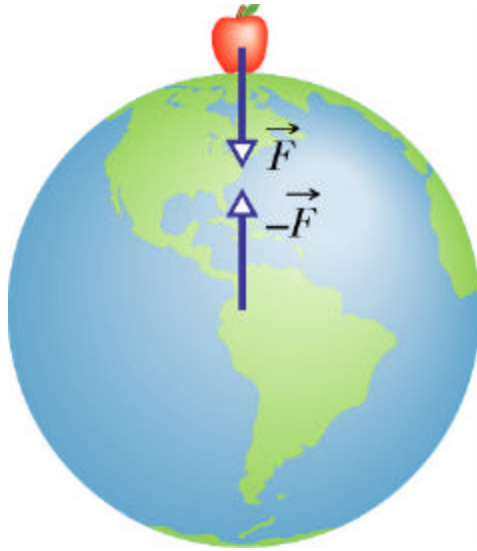
- Radial dependence of density
- Earth rotation reduces effective "weight" but this effect is tiny ($<.034\text{m/s}^2$)
- More important: gravitational force (and acceleration) decrease with R -- but need to go very high to see effect.

$$R_{\text{Earth}} = 6370 \text{ km}$$



Altitude (km)	a_g (m/s^2)	Altitude Example
0	9.83	Mean Earth surface
8.8	9.8	Mt. Everest
36.6	9.71	Highest manned balloon
400	8.7	Space shuttle orbit
35 700	0.225	Communications satellite

Gravity at surface of the Earth



$$G \frac{Mm}{R^2} = mg$$

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M = Earth mass
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 - ◆ Density vs r
 - ◆ Rotation of Earth
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- Recitation session tomorrow will go over the sample midterm